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Rational Ship Speed Trial Evaluation
Rational method proposed
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Results of rational evaluation only!
Results of traditional evaluation
not being disclosed!

**Note! All data in coherent SI units, except time in hr,
 as stored in the corresponding program TID_data.mcd**

Units

$$kn := \frac{1852 \cdot m}{3600 \cdot sec}$$

$$MW := 10^6 \cdot watt$$

Trial identification TID := "05010"

File_const := concat(TID, "_const.prn")

Const := READPRN(File_const)^T

Const₀ := TID TID = "05010" ρ := Const₁ D := Const₂

Measured data: Physical data for traditional runs as provided by the yard

File_meas_trad := concat(TID, "_meas_trad.prn")

Data_meas_trad := READPRN(File_meas_trad)

t := Data_meas_trad^{<0>} φ := Data_meas_trad^{<1>} V_Grd := Data_meas_trad^{<2>}
 N_Shaft := Data_meas_trad^{<3>} P_Shaft := Data_meas_trad^{<4>}
 V_W.rel.abs := Data_meas_trad^{<5>} V_W.rel.dir := Data_meas_trad^{<6>}

Convention: Speed over ground is assumed to be given in the direction of the course!

Identification of models

n := rows(t) n = 8 Size of sample

i := 0..n - 1

Power characteristic in the behind condition

$$A_{rat_{i,0}} := (N_{Shaft_i})^3$$

$$A_{rat_{i,1}} := - (N_{Shaft_i})^2 \cdot V_{Grd_i}$$

Convention: This model is introduced as sufficient approximation

Current velocity in the range of the data available.

Harmonic current model

T := 12·hr + 25·min

Average cycle of tides

$$\omega := \frac{2 \cdot \pi}{T}$$

$$\omega = 1.406 \cdot 10^{-4} \text{ sec}^{-1}$$

$$\omega := \omega \cdot \text{hr}$$

$$\omega = 0.506$$

$$D_{\text{Curr}_i} := \text{if}(\phi_i < \pi, -1, 1)$$

Direction of current

$$A_{\text{rat}_{i,2}} := (N_{\text{Shaft}_i})^2 \cdot D_{\text{Curr}_i}$$

$$A_{\text{rat}_{i,3}} := A_{\text{rat}_{i,2}} \cdot \cos(\omega \cdot t_i)$$

$$A_{\text{rat}_{i,4}} := A_{\text{rat}_{i,2}} \cdot \sin(\omega \cdot t_i)$$

Least square fit

$$X_{\text{rat}} := \text{LI}(A_{\text{rat}}) \cdot P_{\text{Shaft}}$$

Residua in terms of power

$$E := P_{\text{Shaft}} - A_{\text{rat}} \cdot X_{\text{rat}}$$

Relative residua

$$e_i := \frac{E_i}{P_{\text{Shaft}_i}}$$

Quality of approximation

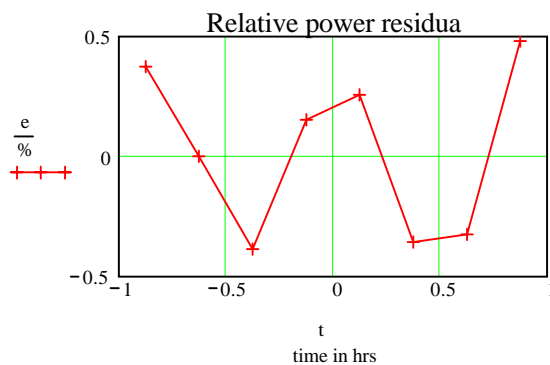
$$\frac{|E|}{|P_{\text{Shaft}}|} = 0.305 \%$$

Left-inverse

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LI(A) :=
  r ← rows(A)
  c ← cols(A)
  s ← svds(A)
  for i ∈ 0..c - 1
    ISVi,i ← (si)-1
  UV ← svd(A)
  U ← submatrix(UV, 0, r - 1, 0, c - 1)
  V ← submatrix(UV, r, r + c - 1, 0, c - 1)
  Ainv.left ← V · ISV · UT
  Ainv.left

```



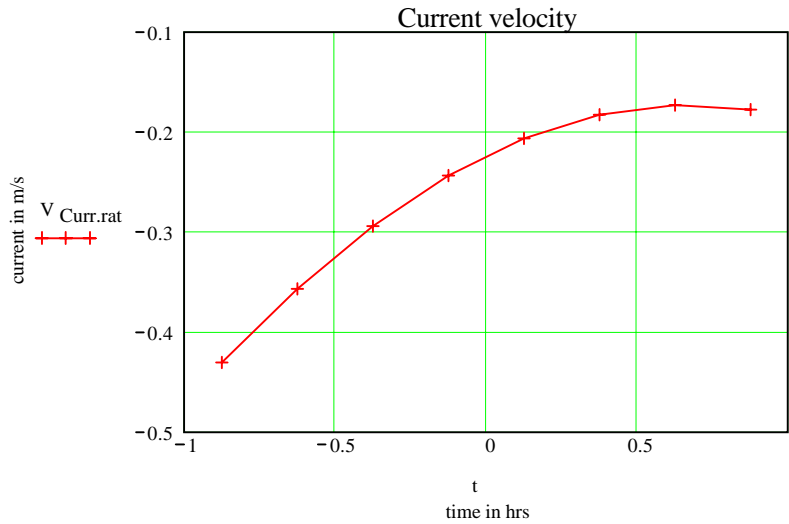
Current velocity

$$j := 0..2$$

$$v_j := \frac{X_{\text{rat}_{2+j}}}{X_{\text{rat}_1}}$$

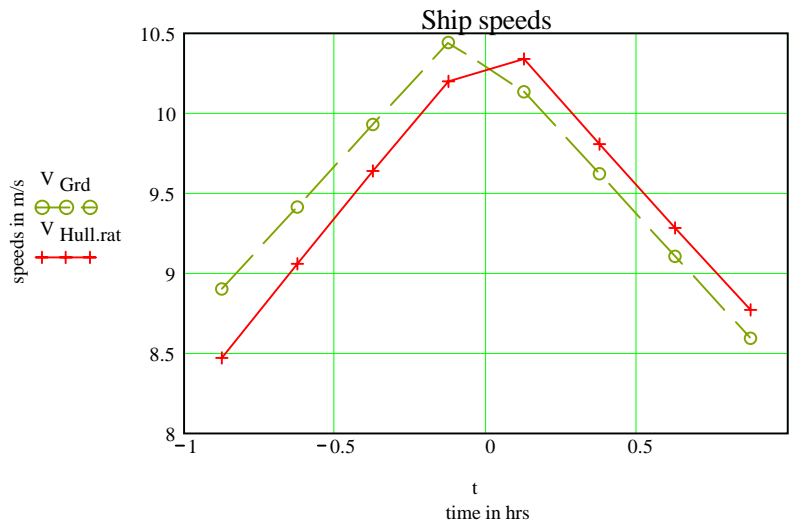
$$V_{\text{Curr.rat}_i} := v_0 + v_1 \cdot \cos(\omega \cdot t_i) + v_2 \cdot \sin(\omega \cdot t_i)$$

Convention: The current is assumed to be in the direction of the ship's axis, the propeller is assumed not to notice cross flow.



Ship hull speed, i. e. relative to the water

$$V_{Hull.rat_i} := V_{Grd_i} - V_{Curr.rat_i} \cdot D_{Curr_i}$$



Power parameters, rational

$$P_{rat_0} := X_{rat_0} \quad P_{rat_1} := X_{rat_1}$$

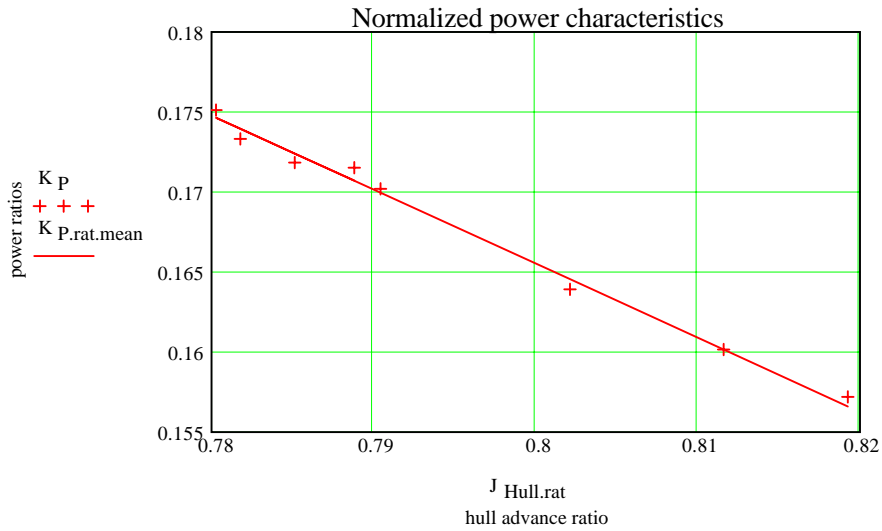
Normalised values

$$J_{Hull.rat_i} := \frac{V_{Hull.rat_i}}{D \cdot N_{Shaft_i}} \quad K_{P.rat_0} := \frac{P_{rat_0}}{\rho \cdot D^5} \quad K_{P.rat_1} := \frac{P_{rat_1}}{\rho \cdot D^4}$$

Power characteristic

$$K_{P.rat.mean_i} := K_{P.rat_0} - K_{P.rat_1} \cdot J_{Hull.rat_i}$$

$$K_{P_i} := \frac{P_{Shaft_i}}{\rho \cdot D^5 \cdot (N_{Shaft_i})^3}$$



'Resistance' characteristic

$$i := 0..n - 1 \quad V_{W.rel.x_i} := V_{W.rel.abs_i} \cdot \cos(V_{W.rel.dir_i})$$

$$k := 0..2 \quad A_{req_{i,k}} := (V_{Hull.rat_i})^{k+1} \quad A_{req_{i,3}} := (V_{W.rel.x_i})^3$$

Convention: This model is introduced as sufficient approximation

$$X_{req} := LI(A_{req}) \cdot P_{Shaft} \text{ of the data available.}$$

$$E_{req} := P_{Shaft} - A_{req} \cdot X_{req}$$

$$e_{req_i} := \frac{E_{req_i}}{P_{Shaft_i}}$$

Quality of approximation

$$\frac{|E_{req}|}{P_{Shaft}} = 1.049\%$$

Final rational power

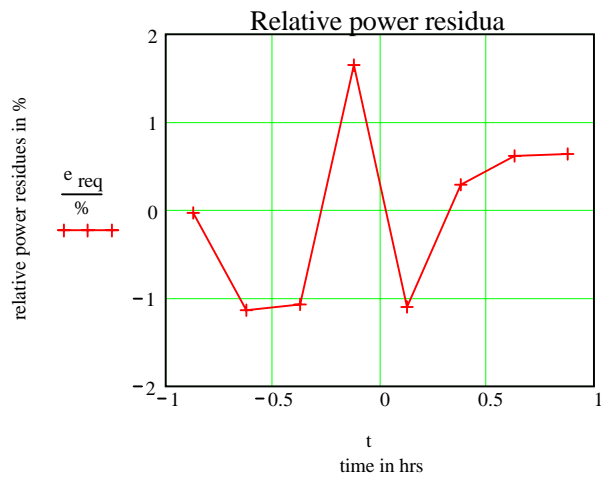
$$V_{W.red.x} := -V_{Hull.rat}$$

$$A_{red.3_i} := (V_{W.red.x_i})^3$$

$$P_{Shaft.rat.fin} := A_{req} \cdot X_{req} - X_{req_3} \cdot A_{req}^{<3>} + X_{req_3} \cdot A_{red.3}$$

Table of values

Speed	Speed_Power _{0,0} := "Speed in kn"	
	Speed _i := (16.5 + 0.5 · i) · kn	Speed_Power _{i+1,0} := $\frac{Speed_i}{kn}$
Power	Speed_Power _{0,1} := "Power in MW"	



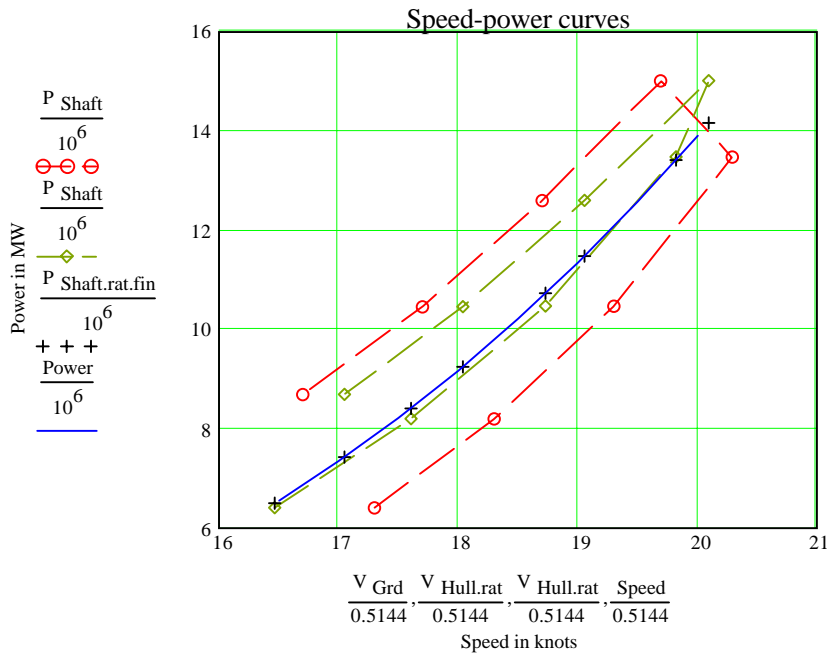
$$A_{red_{i,k}} := \left(\frac{Speed_i}{m \cdot sec^{-1}} \right)^{k+1}$$

$$A_{red_{i,3}} := \left(\frac{-Speed_i}{m \cdot sec^{-1}} \right)^3$$

$$Power := A_{red} \cdot X_{req}$$

$$Speed_Power_{i+1,1} := \frac{Power_i}{10^6}$$

	"Speed in kn"	"Power in MW"
Speed_Power =	16.50	6.56
	17.00	7.35
	17.50	8.22
	18.00	9.18
	18.50	10.22
	19.00	11.36
	19.50	12.59
	20.00	13.91



Rates of revolution

```

Revs(p, V, P, N) :=
  n_i ← last(V)
  for i ∈ 0..n_i
    q_0 ← P_i
    q_1 ← V_i
    n ← N_i
    N_rat_i ← root(q_0 - p_0 · n^3 + p_1 · n^2 · q_1, n)
  N_rat
    
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$$N_{\text{Shaft.rat.fin}} := \text{Revs}(p_{\text{rat}}, V_{\text{Hull.rat}}, P_{\text{Shaft.rat.fin}}, N_{\text{Shaft}})$$

Table of values

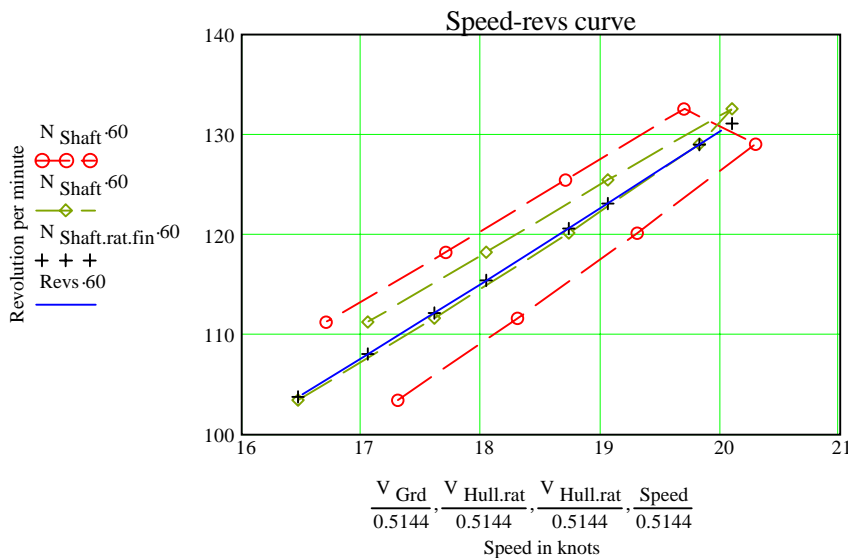
Speed $\text{Speed_Revs}_{0,0} := \text{"Speed in kn"}$ $\text{Speed_Revs}_{i+1,0} := \frac{\text{Speed}_i}{\text{kn}}$

Revolutions $\text{Speed_Revs}_{0,1} := \text{"Revs per min"}$

$$\text{Revs} := \text{Revs}(p_{\text{rat}}, \text{Speed}, \text{Power}, N_{\text{Shaft}})$$

$$\text{Speed_Revs}_{i+1,1} := \text{Revs}_i \cdot 60$$

	"Speed in kn"	"Revs per min"
Speed_Revs =	16.50	104.00
	17.00	107.65
	17.50	111.34
	18.00	115.07
	18.50	118.84
	19.00	122.64
	19.50	126.47
	20.00	130.32



Remarks: All conventions are open for discussion.
The sea state has not yet been taken into account
 for lack of an adequate model,
 that may be identified from the few data at hand
 due to the traditional trials procedure.
Errors due to incorrect interpretation of the traditional
conventions may still have to be corrected!!!

END Rational Ship Speed Trial Evaluation